Regional Simulation Model (RSM) Management Simulation Engine (MSE)

Version 2.2.9

Supervisors

Documentation and User Manual

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Abstract

This document provides descriptions and documentation of supervisory control facilities implemented in the Management Simulation Engine (MSE) component of the Regional Simulation Model (RSM).



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1 Introduction

The Regional Simulation Model (RSM) is a comprehensive hydrological model intended to serve the numerical modeling needs of the South Florida Water Management District. RSM incorporates an object-oriented design approach, leveraging the inherent advantages of logical abstraction, inheritance, and hierarchical data object organization throughout the model. The RSM consists of two interactive, primary components:

- 1. Hydrologic Simulation Engine (HSE)
- 2. Management Simulation Engine (MSE)

The HSE is a finite volume, coupled surface/groundwater/canal numerical model with full 2D and partial 3D flow capability. HSE includes structure flow equations for a wide variety of control structures, and implements efficient numerical solutions of conjunctive hydrological simulations [1, 2, 3].

The MSE is designed to simulate the operational control characteristics encompassed by the wide spectrum of water flow control structures and algorithms currently in use. The MSE is comprised of two primary subcomponents:

- 1. Controllers
- 2. Supervisors

The controllers are a suite of low-level control algorithms which serve as flow regulators for individual structures. The controllers are defined within the RSM XML model file <controller> tag environment, and are detailed in a separate document [4]. The supervisors comprise a set of high-level supervisory control functions which provide dynamic controller modification and coordination intended to facilitate regional control objectives. The supervisors therefore enable regional and subregional operational policy simulation in the RSM by interacting with, and controlling the behavior of the watermover controllers. Each supervisor must be defined in the RSM XML input file within the <management> tag environment. This document provides development, implementation, and usage details for the MSE supervisors.

MSE is intended to provide two major modes of functionality in assisting the hydrological modeler involved in analysis and prediction of water control structure operational behaviors:

- Simulate existing water resource policies: Assessment of currently implemented management operational policies in response to hydrological forcing.
- Develop alternative resource control strategies through the optimization of operational policies.

The first task is a critical capability for the assessment of water control operations in response to historic, real-time, or forecast forcing conditions. In this mode the MSE modifies the behavior of the controllers to achieve a predefined subregional or regional water resource allocation. Elucidation of the imposed watermover flows can then be used to develop appropriate operational policies consistent with the available resources and desired objectives. The latter facility forms an important analysis tool aimed at identification of alternative operational policies which must perform complex, multi-variate, resource allocation functions under the control of system boundary conditions and constraints. The MSE is formulated to address both of these needs by providing a flexible, extensible, and interoperable suite of supervisory processors such as a rule-based expert system and a generic mathematical programming language interface which provides access to a suite of state-of-the-art optimization algorithms.

1.1 RSM Architecture

A schematic representation of the RSM information processing architecture is depicted in figure 1. The HSE reads boundary condition information concerning the spatial characteristics of the model from the cell mesh (.2dm), canal network (.map), and associated initial head and flow files. Input information also may be obtained from rainfall, ET, or other hydrological process coverage/timeseries files. Based on this information HSE computes flow and water levels for each component of the model at each timestep. This comprises a set of state information (Σ), which describes the hydrological response of the system to the imposed boundary conditions and forcing functions.

For the purposes of water management decisions, it may appropriate to process the hydrological state information (Σ) with a variety of filters such as spatio-temporal expectations, spatio-temporal integration/differentiation, or timeseries amplitude or phase modulations. These operations are performed by the Assessors and Filters. Assessors are specialized data processing algorithms suited to particular needs of water resource management, such as assessing the water supply needs for a water control unit (WCU). Currently,

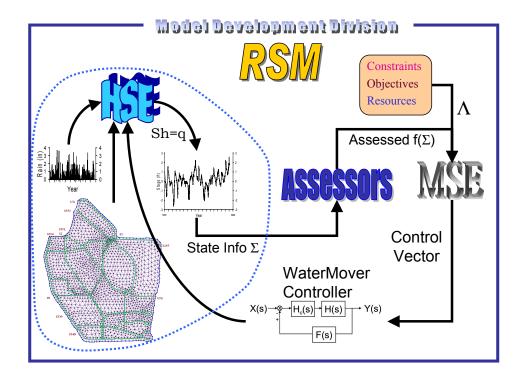


Figure 1: RSM Schematic

the Assessors are still in development, and are not documented. Refer to the Benchmarks for the latest usage and implementations of Assessors. Filters are generic data processors intended to provide common data preprocessing functions such as scalar or timeseries amplitude modulation consisting of the usual arithmetic operations (multiplication, division, addition, subtraction) or may compute simple timeseries or spatial variable statistics such as arithmetic, geometric, or other expectations, or may act as an accumulator. Information on filters may be found in the MSE Controllers Manual [4] in section Data Monitor Filters.

The MSE accesses any raw, assessed, or filtered state information through a <*monitor> interface. Based on the hydrological state information, as well as any needed supervisory or control information, the MSE sets controller variables for each supervised controller. The controller then modulates the maximum available flow of the HSE watermover.

1.2 MSE Architecture

The MSE is tasked with a multi-dimensional objective function resolution based on finite resource allocations and (possibly) interactive, multi-variate constraint imposition. This task sounds complex, and it is. To achieve this in a generalized, algorithmic independent implementation requires significant complexity in the design of the MSE. Nonetheless, it is intended that utilization of industry standardized rule-base formulations, mathematical programming language interpreters, and application specific heuristic supervisory algorithms can serve to isolate the modeler from such complexity.

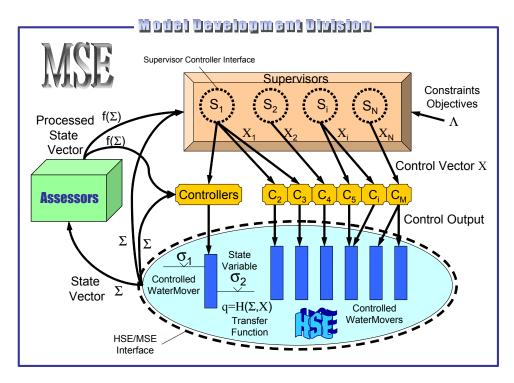


Figure 2: MSE Schematic

The MSE design approach is to allow multiple, independent supervisory control or objective optimization algorithms to run in parallel. The supervisors are mapped to individual, or multiple controllers, providing a high level of flexibility in the configuration of control policies. It is notable that this design allows for the investigation of regional water policy management decisions with implicit consideration of fully coupled hydrological flows and managed structure behaviors. A schematic representation of the

MSE information flow structure is shown in figure 2.

MSE will receive state information from the HSE, as well as constraint and objective information (Λ) from the user defined inputs. MSE supervisors compute a control vector (X) which is applied to the appropriate controllers. A supervisor is capable of controlling a single, or multiple controllers, and multiple controllers can be attached to a watermover, though only one controller at a time can modulate the watermover.

It is relevant to note that this information processing scheme does not specify, or rely upon a particular form of the control decision generator. The implementation of a uniform interface between the supervisors and controllers, and between the controllers and watermovers means that controllers and supervisors are interoperable, and may be dynamically switched. This observation forms a core motivation for design of the MSE information processing facilities as an algorithmic independent implementation. In this manner, maximum extensibility and flexibility is retained for the application of existing or future resource allocation or policy optimization schemes.

2 Supervisory Control of Controllers

The MSE supervisor is effectively a meta-controller, a controller of controllers. It is therefore important to understand the essential implementation details of the MSE controllers, significantly, the controllers are implemented as flow control regulators. The output of the controller is applied as an amplitude scale factor to the computed flow of the watermover. The intended range of controller outputs is in the interval of [0,1]. The user may define the control output range for all of the controllers except the Sigmoid controller. The user is *strongly cautioned* that implementation of controllers with output control ranges outside of the interval [0,1] may result in unintended modulation of watermover flow values. The output control value may be interpreted as a percentage of the total allowable structure flow.

MSE supervisors have the ability to change individual response characteristics of the MSE controllers, or, in the case of multiple controllers attached to a watermover, to select and activate a specific controller for a watermover. The available meta-control attributes for each controller are described in section 2.1. However, it is notable that all controllers implement the control XML attribute which is used to activate/deactivate the controller. If the value of control is set to any value other than ''on'', the controller will be deactivated. This means that the control output will be forced to a value of 1, no control output variations will occur. Since the control outputs are applied as amplitude modulation factors to the watermover flow, the watermover flow will default to it's uncontrolled values.

It is worth noting that there is a special 'controller' dedicated solely to Linear Programming (LP) supervisory control, the <lpctrl> controller. The purpose of this controller is to provide a transparent interface from a LP supervisory control variable to control of a watermover flow. The <lpctrl> controller therefore has no control algorithm and does not process state information. The <lpctrl> controller simply links a LP supervisor output variable to a watermover flow such that the value of the supervisor output variable directly scales (multiplies) the watermover flow value.

Description and implementation details of the MSE controllers can be found in the MSE Controllers Manual [4].

2.1 Controller Functional Attributes

Each controller has specific attributes which may be controlled by the supervisor. The interface to these functions is specified with the func= attribute of the <varOut> supervisor tag, see section 7. Generally, there is a func=

attribute which directly corresponds to an XML attribute of the controller definitions. For example, the Setpoint controller has an attribute setlow= as shown here:

<setpointctrl cid="125" wmID="25" label="S38 Culvert" setlow="0.">

The exact same effect can be achieved by the supervisor by specifying an output variable with a value of 0 that is linked to the func="setLow". Sections 2.1.1 - 2.1.8 define the allowed functional attributes for each controller. Refer to the RSM Controllers Manual [4] for descriptions of the individual controller functional attributes.

2.1.1 General Controller Function XML

In addition to the controller specific functions, all controllers share some common functions that can be controlled by the supervisor. These common functions and values are shown in Table 2.1.1.

attribute	value	meaning
func=		
controlOn	0 or 1	on or off
ctrlMin	[0, 1]	minimum output
ctrlMax	[0, 1]	maximum output

Table 2.1.1. Common Controller Functions

If the value of controlOn is set to any value other than 1, the controller will be deactivated. This is directly analogous to the control='off' XML attribute in the controllers XML definition. If the controller is deactivated, the control output will be forced to a value of 1, no control output variations will occur. Since the control outputs are applied as amplitude modulation factors to the watermover flow, the watermover flow will default to it's uncontrolled values.

The ctrlMin and ctrlMax attributes will set the minimum and maximum controller output limits. The user is cautioned to exercise care in setting these values outside of the interval [0, 1].

2.1.2 Fuzzy Controller Function XML

attribute	value	meaning		
func=				
newControl	0 or 1	reset controller		
FCLFile	string	new FCL file name (Not Implemented)		

Table 2.1.2. Fuzzy Controller Functions

2.1.3 Setpoint Controller Function XML

attribute	value	meaning
func=		
setpoint	\Re	constant setpoint
setlow	\Re	low setpoint
sethigh	\Re	high setpoint
triglow	\Re	low trigger
trighigh	\Re	high trigger
window	0, 1, 2	outside, inside, all
trigger	0 or 1	off or on
step	0 or 1	down or up

Table 2.1.3. Setpoint Controller Functions

2.1.4 Sigmoid Controller Function XML

attribute	value	meaning
func=		
offset	\Re	target offset
Gi	\Re	integral term gain
Gp	\Re	proportional term gain
integral	\Re	error integral
c	\Re	sigmoid parameter
scale	\Re	output scale factor
type	0 or 1	negative or positive
target	\Re	new target
error	\Re	error integral

Table 2.1.4. Sigmoid Controller Functions

2.1.5 PID Controller Function XML

attribute	value	meaning
func=		
offset	R	target offset
Gi	\Re	integral term gain
Gd	\Re	derivative term gain
Gp	\Re	proportional term gain
integral	\Re	error integral
type	0 or 1	negative or positive
target	\Re	new target
error	\Re	error integral

Table 2.1.5. PID Controller Functions

2.1.6 User Controller Function XML

attribute	value	meaning
func=		
newControl	0 or 1	reset controller
module	shared object name	string (Not Implemented)
func	control function name	string (Not Implemented)

Table 2.1.6. User Controller Functions

2.1.7 LP Controller Function XML

attribute	value	meaning
func=		
ControlOut	\Re	control value
TargetFlow	\Re	LP desired flow (cfs)

Table 2.1.7. LP Controller Functions

2.1.8 Alpha Controller Function XML

attribute	value	meaning
func=		
fullopen	R	control cutoff
alpha	\Re	control parameter
offset	\Re	target offset
nvals	int	no. integration points
target	\Re	new target

Table 2.1.8. Alpha Controller Functions

2.2 Multiple Controller Selection

Implementation of generic, nonlinear field controllers, such as those commonly employed by the District, may be difficult to achieve with a single control algorithm per structure. The MSE controllers therefore support the notion of 'controller overloading'. This means that more than one controller may be attached to a watermover. The intention is that separate controllers with distinct control response characteristics may be enabled in varying state-variable regimes suitable to each controller. For example, a simple piecewise linear transfer function may be used under dry conditions, while a rule based expert system (fuzzy) controller may be more effective in flood conditions. A MSE supervisor can select and activate one of multiple controllers attached to a watermover.

Note that the MSE to HSE controller interface does not allow multiple, concurrent controllers to provide flow modulation commands to a water-mover. Although multiple controllers may be attached to a watermover, and can perform control algorithm computations concurrently (in the same timestep) only one controller per timestep will have it's control output applied to a watermover. It is the user's responsibility to ensure that multiple controllers are supervised accordingly.

When multiple controllers per watermover are initially parsed and created from the XML model file specifications, the first controller that is parsed will be set as the active controller for the watermover. Subsequently, controllers that are encountered for the same watermover will replace the existing active watermover if the controller attribute control="on" is set.

Examples of a user defined supervisor activating single controllers from multiple watermover controllers are shown in section 8.10.

2.2.1 Multiple Controller Selection XML

attribute	value	meaning
func=		
controller	\Re	controller $id > 0$

Table 2.2.1. Multiple Controller Selection XML

2.3 Controller Override

It may be desirable for a supervisor to directly control the flow modulation of a watermover. To accommodate this the supervisors are able to directly 'override' the control computations of a watermover controller. This is done with the use of the func="" attribute of a supervisor a <varOut> environment set to either func="controlOut" or func="override".

If the <varOut> specifies func="controlOut", then the controller output will be replaced by the value of the supervisor <varOut>. As an example:

<varOut ctrlID="103" func="controlOut" name="Override"> </varOut>

The above <varOut> will force the controller to apply the output value of the supervisor variable named "Override" to the watermover flow modulation. Setting func="controlOut" implicitly sets the override on for future timesteps. The supervisor will continue to override the controller output value until this feature is 'turned-off'. In order to turn-off (or turn-on) the controller override, the supervisor implements a <varOut> which sets the attribute func="override" and assigns it 0 for off, 1 for on. An example of this usage is shown below.

<varOut ctrlID="103" func="override" name="OverrideOnOff"> </varOut>

The above <varOut> will activate the controller override for controller ctrlID="103" if the value of <varOut name="OverrideOnOff"> evaluates to non-zero. This assumes that a supervisor has previously activated a controller override for this controller with the func="controlOut" attribute. If the <varOut name="OverrideOnOff"> value evaluates to zero, then the controller override is deactivated, and the control value computed by the controller will be applied to the watermover modulation.

2.3.1 Controller Override XML

attribute	value	meaning
func=		
override	0, 1	0-off 1-on
controlOut	\Re	control value

Table 2.3.1. Controller Override XML

3 MSE Network

An important feature of the MSE in general is the usage of Assessors and the MSE Network to provide synoptic state variable inputs for the controllers and supervisors. The MSE Network is an abstraction of the canal network and water control structures based on graph theory. It provides implicit aggregation of HSE canal network segments into Water Control Units (WCU's). The WCU is an integrated data object which stores assessed values of state variables relevant to the collection of HSE segments. Through the use of assessors and monitors, the controllers and supervisors access this synoptic information. The MSE Network also contains information relevant to management policies of the WCU's, and operational characteristics of the structure watermovers. The MSE Network is fully described in the RSM Controllers Manual [4] in section MSE Network.

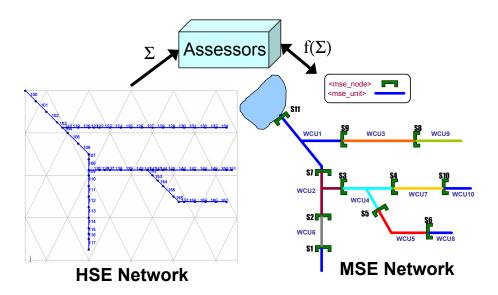


Figure 3: HSE & MSE Network

4 Input Variables

The <varIn> XML environment provides a generic interface for the multiinput variables accessed by MSE supervisors. The XML attributes and environments supported by <varIn> are shown in Table 4.

environment	attribute	meaning
<pre><varin></varin></pre>		input variable(s)
	name	input variable name
	source	input source
	monitor	monitor specification
	monID	monitor ID
	monType	monitor type
	param	parameter name for GLPK
	${ m mse_unit}$	MSE Network unit (WCU) name
	$unit_attr$	MSE Network mse_unit attribute
	mse_arc	MSE Network arc name
	arc_attr	MSE Network mse_arc attribute
	mse_node	MSE Network node name
	$node_attr$	MSE Network mse_node attribute
<scalar></scalar>		single value XML input
<vector></vector>		multi value XML input
<matrix></matrix>		2D value XML input

Table 4. varIn Tags

The <varIn> environments define the state input(s) and provide a link between the inputs defined in the XML file and the RSM state variables. The name= argument defines a key which is used to access an input state variable. Each <varIn> entry can have one of three source= attributes which defines the source of the data input: "monitor", "xml" or "mse_network". The default is source="monitor".

4.1 RSM Monitor Inputs

To input state information from a RSM monitor interface (i.e. <segmentmonitor>) set the source="monitor", or omit the source= attribute. In this case the varIn will have an associated <*monitor> entry. The monitor=, monID= and monType= attributes must match the attributes of the associated state <*monitor>. For example, the following are valid XML entries for a varIn and monitor pair:

However, if the monitor is a timekeeper monitor (<tkprmonitor>), the monID= attribute is not used. The timekeeper monitor does not use the id attribute as do the other state monitors. An example of this invocation would be:

4.2 XML Inputs

To define 'static' input variables directly in the XML of the varIn, set source="xml". Three variable formats are supported: scalar, vector, matrix. The scalar is simply a single data value. A vector is a one-dimensional list of values, and the matrix is a two-dimensional table of columns and rows. Within a single varIn environment one XML input variable environment may be created as shown below:

Vector datamembers are delimited by whitespace. Matrix columns (members of a row) are delimited by whitespace. Matrix rows are delineated by ';' or ','. All vector and matrix indices follow C/C++ semantics: 0 is the first element. To access these members from a user defined supervisor, several interface functions are provided as described in the MSE Controllers Manual [4] in section C++ User Controller API functions. The XML inputs are currently only supported for C++ user defined controllers and supervisors.

4.3 MSE Network Inputs

The supervisor can also obtain input variables from objects of the MSE Network (see section MSE Network of the MSE Controllers Manual [4]). Any variable that is contained in an mse_unit, mse_arc or mse_node can be accessed. Currently, only the User Defined supervisor is capable of accessing these values through the use of API function calls. Sections C++ User Controller API functions and MSE Network XML in the MSE Controllers Manual [4] provide details and examples on the usage of these functions.

5 Output Variables

The varOut environment is used to couple the (possibly multiple) output of a supervisor function to the appropriate controller or watermover. The XML attributes and environments supported by <varOut> are shown in Table 5.

environment	attribute	meaning
<varout></varout>		output variable(s)
	ctrlID	controller ID
	wmID	watermover ID
	func	controller function
	name	output variable name
<pre><*monitor></pre>		State variable specification

Table 5. User Defined Supervisor System XML

Each varOut must have either the ctrlID or wmID defined, but not both. The ctrlID is used when a supervisor is setting a controller attribute as described in section 2.1. The wmID is used only when a supervisor is selecting a controller for activation on a watermover. For example, in the following excerpt the first varOut is selecting a controller, while the second and third are setting a controller functional attribute.

```
<varOut wmID="2" func="controller" name="s4_Controller"> </varOut>
<varOut ctrlID="103" func="triglow" name="103_TrigLow"> </varOut>
<varOut ctrlID="104" func="triglow" name="104_TrigLow"> </varOut>
```

The func attribute is used to specify which controller functional attribute is being modified. The allowed values of this attribute are described in section 2.1. The name attribute must correspond to the name of the supervisor function in user defined modules, or to the output variable name in the FCL file of fuzzy supervisors or the output variable name of a GLPK supervisor. Refer to the section of a particular supervisor for usage and examples of varOut.

6 Supervisor Monitors

MSE uses the <spvrmonitor> environment to monitor input state values fed to the supervisors, or to monitor output values generated by supervisors. To monitor controller I/O, and watermover variables, the user may resort to the <ctrlmonitor> and <wmmonitor> environments respectively. These monitors are detailed in the MSE Controllers Manual [4] within the Watermover Control & Maxflow Monitors, and the Controller Monitors sections. The <spvrmonitor> attributes are shown in Table 6.

environment	attribute	meaning
<pre><ctrlmonitor></ctrlmonitor></pre>		
	spvrID attr	ID of supervisor to be monitored attribute to be monitored
	montype	type of variable: scalar, vector
	var	variable name for type vector

Table 6. Supervisor Monitor XML

Each supervisor monitor must define a spvrID="" attribute of the <spvrmonitor>. The spvrID attribute specifies supervisor id number of the supervisor to be monitored. The spvrID must be a positive integer. The other required attribute is the attr="". The attr="" may take one of two values: "output" or "state", which are used for supervisor output and input monitoring respectively.

Generally, supervisors are multi-input/multi-output (MIMO), though they can be single-input/single-output. The montype="" attribute specifies whether the data stream is single or multi I/O by assignment of the values scalar (default) or vector respectively. In the case of multi-inputs or outputs, the var="" attribute is assigned the varIn or varOut name of the corresponding variable.

Examples of supervisor monitors for output to dss files are shown below. The first example outputs the supervisor output variable ctrl_103_TrigLow, while the second entry writes the supervisor input variable segment1Head.

An example of a supervisor monitor is shown below for a User supervisor that is monitoring the output value of another supervisor.

7 Supervisors: General Usage

The supervisors that are currently available within the MSE are:

- User Defined Finite State Machine, section 8
- Expert System Rule Base (Fuzzy), section 9
- Linear Programming Optimization, section 10
- Graph Flow Algorithm, section 11
- ORM, section 12

Each supervisor must be defined in the RSM XML input file in the <management> environment. Within the <management> section, the supervisors are defined with appropriate XML specifications. The XML environments available for the MSE supervisors are shown in Table 7.

environment	meaning
<user_supervise></user_supervise>	User defined finite state machine
<fuz_supervise></fuz_supervise>	FCL rule-based expert system
<pre><glpk_supervise></glpk_supervise></pre>	GNU Linear Programming Kit
<pre><orm_supervise></orm_supervise></pre>	Object Routing Model
<pre><graph_supervise></graph_supervise></pre>	Graph theory flow algorithms

Table 7. MSE Supervisor XML

General supervisory control XML for activation/deactivation of supervisors, or conditional supervisor execution are described below in sections 7.1 and 7.2.

7.1 Global Supervisor On/Off

It may be advantageous to deactivate all supervisors with a single variable. This is the function of the supervisors variable in the <control> section of the XML input file. The default value is supervisors="on". If the value is set to any value other than "on", all supervisors will be deactivated. The supervisors will not influence the behavior of the controllers, the controllers will operate according to their internal algorithms or rules. An example of this usage is shown below.

```
<control
  tslen="15"
  tstype="minute"
  startdate="01jan1994"
  starttime="1200"
  enddate="05jan1994"
  endtime="0600"
  alpha="0.500"
  solver="PETSC"
  method="gmres"
  precond="ilu"
  controllers="on"
  supervisors="off">
</control>
```

7.2 Supervisor Time Interval

Execution of supervisory control may not be required at each timestep of the simulation, in which case the user may specify a simulation time interval which must elapse in order for the supervisor to be activated. This interval is set within the supervisors XML tag specification via the attributes shown in Table 7.2.

attribute	type	meaning
days	int	number of days in interval
hours	int	number of days in interval
minutes	int	number of minutes in interval

Table 7.2. MSE Supervisor XML

For example, to set the GLPK supervisor to run at simulation intervals of 3 days, 2 hours and 1 minute, the following XML tag attributes can be used:

```
<management id="1" label="RSM Supervisor">
  <glpk_supervise id="801" label="glpk_supervise_1"
  modelFile="glpk_mse1.mod" days="3" hours="2" minutes="1">
  </glpk_supervise>
</management>
```

The default values are days="0" hours="0" minutes="0", which means that the Supervisor algorithm will run at every timestep.

8 User Defined Supervisor

8.1 Implementation

The user supervisor provides a facility for the user to independently develop a control algorithm applied to a controller/watermover. The user develops a supervisory algorithm in C/C++, then compiles the control routine(s) into a shared object library. The <user_supervise> implements a shared-library loader and function pointer interface which calls the user-defined control function(s) at each timestep. Each <user_supervise> will maintain it's own shared object and function pointer information, allowing the user to define multiple supervisory functions inside a single shared object so that individual supervisors may be enacted by selected functions which reside inside a single shared object. It is also possible to define separate shared objects for each supervisor. The user defined functions can take advantage of several RSM application programming interface (API) functions to assist in accessing input state variables and setting output values. The library function interface is different for C++ and C libraries as described in the following sections. User defined supervisor shared-object codes must include the file mseIO.h.

8.2 XML Interface

Four information items have to be supplied to the supervisor for correct coupling to the RSM state and control information:

- 1. controller id's
- 2. input state variables
- 3. output control variables
- 4. shared library information

this is done with use of the XML attributes available for the user defined supervisor shown in Table 8.2.

environment	attribute	meaning
<pre><user_supervise></user_supervise></pre>		
	id	supervisor id
	label	optional supervisor label
	libType	type of shared object
	module	shared library path name
	func	supervisor function name in module
	xml	MSE Network XML file
	graph	MSE Network graph file
	flow	graph theory solution type
	days	supervise interval in days
	hours	supervise interval in hours
	minutes	supervise interval in minutes
<ctrlid></ctrlid>		list of controller IDs
<varin></varin>		input variable(s)
<varout></varout>		output variable(s)
<pre><*monitor></pre>		state variable to varIn

Table 8.2. User Defined Supervisor System

8.2.1 user supervise attributes

The id is a required, unique supervisor identifier. The label is an optional string which will label the outputs of the supervisor.

The module attribute must specify a valid shared library path name. The func must specify a valid function symbol name contained within the module shared library.

The libType attribute must specify one of the following options:

- C++ (Cpp c++ cpp)
- C (c)

The supervisor time interval control attributes (days hours minutes) provide a mechanism to run the supervisor at selected intervals, see section 7.2.

8.2.2 ctrlID environment

The <ctrlID> environment defines a list of RSM controllers that will be supervised. The values in this list must match a cid= attribute of a valid controller definition. For example, if the following controller is defined:

<setpointctrl cid="125" wmID="25" label="S38 Culvert">

then a valid entry in the <ctrlID> list is 125. Each controller id in the list should have at least one corresponding <varOut> entry which couples the controller modifier with the corresponding function in the shared library. If the supervisor is selecting a controller from among multiple controllers, then there may not be a <varOut> for each entry in the <ctrlID> list.

8.2.3 varIn attributes

The <varIn> environments define the state input(s) and provide a link between the inputs defined in the shared library function and the RSM state variables. The name= arguments define a key which is used in the user-defined function code to access input state variables. Refer to section 4 Input Variables for a description and usage of the <varIn> environment.

8.2.4 varOut attributes

The <varOut> attributes specify which controller is modified by which output variable linked to a shared library module function, or, to activate a single controller for a watermover from among multiple controllers attached to a watermover. Section 5 details the allowable XML entities for <varOut>. In the case where a controller variable is to be changed, the ctrlID attribute is used to specify the controller, the name defines the the output variable function name in the shared library module, and the func specifies the controller variable to be changed. It is possible to have multiple <varOut> entries for a single controller. For example, a supervisor may define three <varOut> terms to modify the on/off, minimum output, and maximum output behaviors of a single controller. Each <varOut> would have a distinct func and name entry. Section 2.1 describes the available func attributes for each controller.

When a supervisor is used to activate a particular controller from among multiple controllers attached to a watermover, the wmID attribute is used to specify the affected watermover, the func="controller" must be set, and the name defines the output variable function name in the shared library module which will return a controller id number (positive integer) of the controller to be activated.

8.3 User Supervisor Criteria

The following criteria apply to the **<user_supervisor>** shared library:

- 1. Ensure that the location of your library is included in the environment variable LD_LIBRARY_PATH
- 2. The function must include the mseIO.h header file.
- 3. The function must include the state_mapIO.cc file to access MSE API functions.
- 4. The function must return an integer value: 0 success, nonzero failure
- 5. C++ shared library functions must accept two input arguments, a pointer to a C++ STL containter: map<string, InputState*>, and a pointer to an map<string, OutputControl*>.
- 6. C shared library functions must accept six input arguments. First is an integer, the number of variables. Second is an array of character pointers, each array element listing an input variable name. Third is an array of floating point double pointers, each reference is to the current state of the corresponding input variable (with the same array index) listed in the array of input variable names. Fourth is the integer number of output variables, fifth an array of character pointers to output variable names, and finally an array of floating point double pointers, each reference to an output variable (with the same array index) listed in the array of output variable names.
- 7. If you compile with a C++ compiler, declare the functions as extern "C" to avoid name mangling in the shared object.

8.4 User Supervisor Library Compilation

To convert C++ code into a shared object with the name UserSpvr.so, assuming that the function is in a file named userspvr.cc, the following command can be used in Linux:

gcc userspvr.cc -Bsymbolic -shared -o UserSpvr.so

8.5 User Supervisor Initialization and Cleanup

If the user desires to have a one-time initialization call, and one-time cleanup call made to the library at the time the library is loaded and unloaded respectively, the user must define two functions within the library:

```
1. void _init() { };
2. void _fini() { };
```

The <code>_init()</code> function will be called after the shared library loader successfully imports the shared library, and the <code>_fini()</code> function will be called before the library is unloaded. To prevent linkage conflicts with common standard library functions, add the -nostdlib argument to the compiler command:

```
gcc userspvr.cc -Bsymbolic -shared -o UserSpvr.so -nostdlib
```

8.6 User Supervisor and Statically Linked HSE

The current version of RSM does not support user defined supervisors developed in C++ if the RSM is statically linked. If the RSM is dynamically linked, then C++ user defined shared libraries are supported.

8.7 C User Supervisor Interface

If the shared library is developed in C, the supervisor functions are called from the MSE with six input variables as shown in the prototype below:

Table 8.7. C user supervisor function prototype

The first argument is an integer which defines the number of input variables being passed to the function. This corresponds to the number of <varIn> variables defined within the <user_supervise> section of the xml file. The second argument is an array of character strings. Each array element contains the name of an input variable as defined in the <varIn name=""> section of the xml file. The third argument is an array of floating point (double) values, which contain the current numerical values of the state variables. The array indices of the second and third arguments match on a one-to-one correspondence. That is, for the variable with the name varInNames[2], the current state value is contained in varInValues[2].

The fourth argument is the number of output variables, which corresponds to the number of <varOut> variables defined within the <user_supervise> section of the xml file. The fifth argument is an array of character strings. Each array element contains the name of an output variable as defined in the <varOut name=""> section of the xml file. The sixth argument is an array of floating point (double) values, which are used to contain the output value computed by the supervisor. The array indices of the fifth and sixth arguments match on a one-to-one basis. That is, for the variable with the name varOutNames[2], the output value is set into varOutValues[2].

The fact that the user has to properly track and access these I/O pointers makes the C function interface hazardous. It is safer and less error-prone to rely on the C++ user interface wherein the assignment of <varOut> values is performed with a function call to the API function SetVarOut(), refer to section 8.9.1.

The supervisor functions must return an integer (int) status value. A value of 0 indicates no error, a non-zero return value indicates that an error has occurred in the supervisor function, in which case a MseError exception will be thrown, and the simulation terminated.

8.8 C++ User Supervisor Interface

User defined supervisors developed in C++ receive two input variables which are pointers to an inputStateMap, and an outputControlMap associative array as illustrated in the following prototype.

Table 8.8. C++ user supervisor function prototype

The C++ map pointed to by lpISMap contains pointers to InputState classes, one pointer for each varIn variable defined in the supervisor XML file. The map key to each pointer is the variable name (varIn="") as defined in the userspvr section of the XML file. To access an input state variable the supervisor function calls the GetVarIn() API function as described in section GetVarIn in the MSE Controller Manual. The definition of the InputState structure can be found in the C++ source file: mseIO.h, which is a required header file.

In an analogous fashion, the C++ map pointed to by lpOCMap contains pointers to OutputControl classes, one pointer for each varOut variable defined in the supervisor XML file. The map key to each pointer is the variable name (varOut="") as defined in the userspvr section of the XML file. To assign an output value the supervisor function calls the SetVarOut() API function as described in section 8.9.1. The definition of the OutputControl structure can be found in the C++ source file: mseIO.h.

The C++ supervisors must return an integer value. A return value of 0 indicates no error occurred in the supervisor function. A non-zero return value indicated that an error occurred in the user supervisor function. In this case an MseError exception is thrown by the MSE, ending the simulation.

An example of a user defined supervisor function interface is shown below.

```
#include <map>
#include "hse/src/mseIO.h"
#include "hse/mse_tools/state_mapIO.cc"
extern "C" int MySupervise( map<string, InputState*>
                                                         *lpISMap,
                            map<string, OutputControl*> *lpOCMap ) {
  string func = "MySupervise";
  double spvrOut1 = 0.;
  double spvrOut2 = 0.;
  double h1 = GetVarIn( func, "segment1Head", lpISMap );
  double h2 = GetVarIn( func, "segment4Head", lpISMap );
  // Provide supervsory function based on input state variable
  // Set the output variables
  if ( not SetVarOut( func, "ctrl_101", spvrOut1, lpOCMap ) ) {
   return -1;
  if ( not SetVarOut( func, "ctrl_102", spvrOut2, lpOCMap ) ) {
    return -1;
 return 0;
```

8.9 C++ User Supervisor API functions

MSE provides a set of API functions to be used for the access of input state variables, setting of output state variables, and accessing data members from the MSE Network. With the exception of the SetVarOut function, all user API functions can be used from a controller as well as a supervisor. For this reason, the API functions are documented in the MSE Controllers Manual [4] in section C++ User Controller API functions.

8.9.1 SetVarOut

To set the value of an output variable from a user defined supervisor, the supervisory function makes a call to the SetVarOut function. The SetVarOut function is not used with MSE controllers, as the controllers are MISO (multi

input single output) processors. SetVarOut is used only with MSE supervisors to individually set one of the multiple output variables.

int SetVarOut(string	func,
string	varOutName,
double	controlOut,
map <string, outp<="" th=""><th>utControl*> *lpOutputControlMap);</th></string,>	utControl*> *lpOutputControlMap);

Table 8.9.1. ${\tt SetVarOut()}$ function prototype

The function returns an integer value of either 0 (failure) or 1 (success). The input arguments are described below.

Name	Type	Description
func	string	name of function in
		user library calling
		GetMSENodeVal(), used
		for error reporting
varOutName	string	name of the varOut output
		variable
controlOut	double	numeric output value of
		supervisor to varOut
lpOutputControlMap	*map <string,< td=""><td>pointer to the OutputControlMap</td></string,<>	pointer to the OutputControlMap
	OutputControl*>	passed into the user defined
		supervisor function

Table 8.9.1. SetVarOut() function arguments

An example of <varOut> XML entries from a supervisor are shown below.

```
<!-- This uses wmID to specify a controller via cid output -->
<varOut wmID="1" func="controller" name="wm1_ctrl"> </varOut>
<!-- This uses ctrlID to set specific controller attributes -->
<varOut ctrlID="102" func="triglow" name="ctrl_102"> </varOut>
```

A corresponding C++ supervisory function could be written as shown below.

```
extern "C" int MySupervise( map<string, InputState*>
                                                         *lpISMap,
                            map<string, OutputControl*> *lpOCMap ) {
  string func = "MySupervise";
  double spvrOut1 = 0.;
  double spvrOut2 = 0.;
  // Get input state variables
  double h1 = GetVarIn( func, "segment1Head", lpISMap );
  double h2 = GetVarIn( func, "segment4Head", lpISMap );
  // Provide supervsory function based on input state variable
  // Set the output variables
  if ( not SetVarOut( func, "wm1_ctrl", spvrOut1, lpOCMap ) ) {
    return -1;
  if ( not SetVarOut( func, "ctrl_102", spvrOut2, lpOCMap ) ) {
    return -1;
  return 0;
}
```

In the above XML section and supervisory function, the output of varOut with name="ctrl_102" is used to dynamically assign a controller to the watermover with ID wmID="1". The value of the variable spvrOut1 in the function MySupervise will be converted to an integer, the controller which has an ID matching the integer value of spvrOut1 will be set as the active controller for the watermover with ID wmID="1". The second output, spvrOut2 will be used to set the "triglow" parameter of the controller with the controller ID ctrlID="102".

8.10 User Defined Supervisor Example

In this example the shared object named UserSprv.so (module="./UserSprv.so") is loaded from the current directory to call the supervisor functions: func="SetWM1Controller" and func="SetWM1CtrlTriggers".

The function SetWM1Controller is used to select one of two controllers

(cid="101" or cid="101") for the watermover with wmID="1". The function "SetWM1CtrlTriggers" will set the lower trigger threshold value (triglow) for the controllers.

These functions will receive two input state values named segment1Head and segment4Head. The state variables will reside in an InputStateMap, with keys segment1Head and segment4Head, which are used to access the input values through the GetVarIn() API function. The two controllers attached to watermover 1 are simple linear transfer function (setpoint) controllers. Refer to the Setpoint Controllers section of the MSE Controller Manual [4] for complete descriptions of the controller parameters. The XML controller definitions for this example are:

```
<controller id="1">
 <!-- Multiple controllers per watermover are defined
 <!-- The first controller parsed will be set as the active controller -->
 <!-- Any subsequent controller with control="on" will become the
 <!-- active controller for the watermover.
                                                                          -->
 <!-- To change the active controllers, the supervisor must assign
                                                                          -->
                                                                         -->
 <!-- another controller
 <!-- Controller for discharge from segment 1 -->
 <setpointctrl cid="101" label="SPCtrl 1: " wmID="1" window="all" control="on"</pre>
    setlow="0.0" sethigh="1.0" triglow="500.0" trighigh="505.0" trigger="on">
    <segmentmonitor id="1" attr="head"></segmentmonitor>
  </setpointctrl>
  <!-- Controller for discharge from segment 1 -->
  <setpointctrl cid="102" label="SPCtrl 1A: " wmID="1" window="all" control="on"</pre>
    setlow="0.0" sethigh="0.5" triglow="495.0" trighigh="500.0" trigger="on">
    <segmentmonitor id="1" attr="head"></segmentmonitor>
  </setpointctrl>
</controller>
```

The XML section which defines the supervisors to select the active controller, and to adjust the lower trigger threshold of the controllers is shown below:

```
<management id="1" label="user-multi-control">
  <!-- Select a controller for watermover 1 -->
  <user_supervise id="801" label="SetWM1Controller" libType="C++"</pre>
                  module="./UserSprv.so" func="SetWM1Controller">
     <ctrlID> 101 102 </ctrlID>
     <!-- Input variables to SetWM1Controller -->
     <varIn name="segment1Head" monitor="segmentmonitor"</pre>
            monID="1" monType="head"> </varIn>
     <varIn name="segment4Head" monitor="segmentmonitor"</pre>
            monID="4" monType="head"> </varIn>
     <!-- Input variable monitors from hse to varIn -->
     <segmentmonitor id="1" attr="head"></segmentmonitor>
     <segmentmonitor id="4" attr="head"></segmentmonitor>
     <!-- This uses wmID to specify a controller via cid output -->
     <varOut wmID="1" func="controller" name="segment1_Controller"> </varOut>
  </user_supervise>
  <!-- Set the triglow threshold for controllers 101 & 102 -->
  <user_supervise id="803" label="SetWM1CtrlTriggers" libType="C++"</pre>
                  module="./UserSprv.so" func="SetWM1CtrlTriggers">
     <ctrlID> 101 102 </ctrlID>
     <!-- Input variables to SetWM1CtrlTriggers -->
     <varIn name="segment1Head" monitor="segmentmonitor"</pre>
            monID="1" monType="head"> </varIn>
     <varIn name="segment4Head" monitor="segmentmonitor"</pre>
            monID="4" monType="head"> </varIn>
    <!-- Input variable monitors from hse to varIn -->
     <segmentmonitor id="1" attr="head"></segmentmonitor>
     <segmentmonitor id="4" attr="head"></segmentmonitor>
     <!-- These use ctrlID to set specific controller attributes -->
     <varOut ctrlID="101" func="triglow" name="ctrl_101_TrigLow"> </varOut>
     <varOut ctrlID="102" func="triglow" name="ctrl_102_TrigLow"> </varOut>
  </user_supervise>
</management>
```

To compile this example code into a shared library named UserSprv.so on a Linux platform:

```
gcc usersprv.cc -BSymbolic -shared -o UserSprv.so
```

The c++ code for each of the supervisor functions is shown below.

```
#include <cstdio> // include if you want to use C-style printf
#include <map>
#include "hse/src/mseIO.h"
                                  // THIS FILE MUST BE INCLUDED
#include "hse/mse_tools/state_mapIO.cc" // THIS FILE MUST BE INCLUDED
//-----
// Function SetWM1Controller for selection of watermover 1 controllers
//----
extern "C" double SetWM1Controller(
               map<string, InputState*> *lpInputStateMap,
               map<string, OutputControl*> *lpOutputControlMap ) {
 int status = 0;
 double superviseOut = 0.; // output value
 // Get the current state value for each variable
 double segment1Head = GetVarIn( func, "segment1Head", lpInputStateMap );
 // Select controller id (101 or 102) based on input state variable
 if (...) { superviseOut = 101 }
 else (...) { superviseOut = 102 }
 // Set the output variable
 if ( not SetVarOut( func, "segment1_Controller",
                   controlOut, lpOutputControlMap ) ) {
   status = -1;
 }
 return status;
```

```
//-----
// Function SetWM1CtrlTrigger
//----
extern "C" double SetWM1CtrlTriggers(
              map<string, InputState*> *lpInputStateMap,
              map<string, OutputControl*> *lpOutputControlMap ) {
 int status = 0;
 double superviseOut = 0.; // output value
 // Get the current state value for each variable
 double segment1Head = GetVarIn( func, "segment1Head", lpInputStateMap );
 // Provide control function based on input state variable
         { controlOut = 495.; }
 else if (...) { controlOut = 498.; }
           { controlOut = 500.; }
 if ( not SetVarOut( func, "ctrl_101_TrigLow",
                  controlOut, lpOutputControlMap ) ) {
   status = -1;
 }
 return status;
}
```

9 Expert System Rule Based (Fuzzy) Supervisor

The ability to simulate application of operational rules to water control structures on a regional scale is an important requirement of the MSE. This feature enables the RSM to simulate the actual operational policies in response to historical, real-time, or forecast forcing events beyond the scope of individual control structures which are acting solely to achieve a local objective. Over the span of many years, District personnel have amassed a large and complex knowledge base of operational control guidelines and rules. Application of this knowledge in response to situational environmental conditions constitutes an expert system which optimizes the regional hydrological responses under the constraints imposed by flood control, water supply and environmental concerns. It is therefore important that a natural and efficient mechanism is employed by the MSE to allow for incorporation of expert system control. The MSE achieves this by use of a multi-input, multi-output characteristic field controller, which is implemented according to the International Electrotechnical Commission (IEC) Technical Committee on Industrial Process Measurement and Control, Programmable Controllers [9]. It relies upon a user-defined set of input/output variables, and rules which map the variables to the control functions.

It is important that the format of the rules do not rely upon an obscure or difficult to understand syntax which decouples the natural expression of the existing knowledge base from that of the MSE implementation. For example, if the published guideline for a structure is: "If the upstream head at structure A1 is high, then open the gate" then the corresponding rule in the expert system management should read roughly the same. The obvious way to achieve this is to apply the principles of linguistic processing, which have led to the development of the Fuzzy Control Language (FCL). The FCL provides a natural, common-language interface to the implementation of a nonlinear characteristic field controller, and is ideal for this purpose. The RSM controllers include a fuzzy controller, which resides in an RSM library developed by the Model Development Division. The MSE leverages on the independent control functionality of the FCL library, and uses it to enact a multi-controller supervisory agent.

9.1 Fuzzy Supervisor Usage

The Expert System Supervisor (fuz_supervise) relies on a user-supplied knowledge base to enact controller supervision. Four information items have to be supplied to the supervisor for correct coupling to the RSM state and control information:

- 1. controller id's
- 2. input state variables
- 3. output control variables
- 4. rule base

this is done by use of the XML attributes available for the rule-based expert system (fuz_supervise) shown in Table 9.1.

environment	attribute	meaning
<fuz_supervise></fuz_supervise>		
	id	supervisor id
	label	optional supervisor label
	fcl	name of FCL rule file
	days	supervise interval in days
	hours	supervise interval in hours
	minutes	supervise interval in minutes
<ctrlid></ctrlid>		list of controller IDs
<varin></varin>		input variable(s)
	name	input variable name
	monitor	monitor specification
	monID	monitor ID
	monType	monitor type
<varout></varout>		output variable(s)
	ctrlID	controller ID
	wmID	watermover ID
	func	controller function
	name	output variable name
<*monitor>		State variable specification

Table 9.1. Rule-based Expert System

9.1.1 fuz supervise attributes

The id is a unique supervisor identifier, label is an optional string which will label the outputs of the supervisor. The fcl attribute must specify a valid FCL definition file. The supervisor time interval control attributes (days hours minutes) provide a mechanism to run the supervisor at selected intervals, see section 7.2.

9.1.2 ctrlID environment

The <ctrlID> environment defines a list of RSM controllers that will be supervised. The values in this list must match a cid= attribute of a valid controller definition. For example, if the following controller is defined:

```
<setpointctrl cid="125" wmID="25" label="S38 Culvert">
```

then a valid entry in the <ctrlID> list is 125. Each controller id in the list will have at least one corresponding <varOut> entry which couples the controller modifier with the corresponding specification in the rule (FCL) file.

9.1.3 varIn attributes

The <varIn> define the state input(s) and provide a link between the inputs defined in the FCL file and the RSM state variables. The name= arguments must correspond to VAR_INPUT variables defined in the specified FCL file. Each <varIn> entry will have an associated <*monitor> (i.e. <segmentmonitor>) entry. The monitor=, monID= and monType= attributes must match the attributes of the associated state <*monitor>. For example, the following are valid XML entries:

However, if the monitor is a timekeeper monitor (<tkprmonitor>), the monID= attribute is not used. The timekeeper monitor does not use the id attribute as do the other state monitors. An example of this invocation would be:

9.1.4 varOut attributes

The <varOut> attributes specify which controller is modified by which output variable in the FCL definition, or, activate a single controller for a watermover from among multiple controllers attached to a watermover. Section 5 details the allowable XML entities for <varOut>. In the case where a controller variable is to be changed, the ctrlID attribute is used to specify the controller, the name defines the the output variable name from the FCL file, and the func specifies the controller variable to be changed. It is possible to have multiple <varOut> entries for a single controller. For example, a supervisor may define three <varOut> terms to modify the on/off, minimum output, and maximum output behaviors of a single controller. Each <varOut> would have a distinct func and name entry. Section 2.1 describes the available func attributes for each controller.

When a supervisor is used to activate a particular controller from among multiple controllers attached to a watermover, the wmID attribute is used to specify the affected watermover, the func="controller" must be set, and the name defines the output variable name from the FCL file which will return a controller id number (positive integer) of the controller to be activated. Currently, the fuzzy supervisor can only return floating point values. The natural process of fuzzy inferencing and defuzzification may make precise control of controller id problematic.

The following <management> environment XML excerpt demonstrates the usage of <varOut> to change the behavior (triglow threshold) of two controllers (ctrlID="101" ctrlID="102").

```
<management id="1" label="multi-control">
  <fuz_supervise id="801" label="fuz_sprv" fcl="multictrl_sprv.fcl">
     <ctrlID> 101 102 103 104 </ctrlID>
    <!-- Input variables to multictrl_sprv.fcl -->
     <varIn name="segment1Head" monitor="segmentmonitor"</pre>
            monID="1" monType="head"> </varIn>
     <varIn name="segment4Head" monitor="segmentmonitor"</pre>
            monID="4" monType="head"> </varIn>
     <!-- Input variable monitors from hse to varIn -->
     <segmentmonitor id="1" attr="head"></segmentmonitor>
     <segmentmonitor id="4" attr="head"></segmentmonitor>
     <!-- These use ctrlID to set specific controller attributes -->
     <varOut ctrlID="101" func="triglow" name="seg1_TrigLow"> </varOut>
     <varOut ctrlID="102" func="triglow" name="seg4_TrigLow"> </varOut>
  </fuz_supervise>
</management>
```

9.2 Expert System Supervisor Example

The following example illustrates two rule-based supervisors, one applied to two fuzzy controllers, the other to a setpoint controller. The fuzzy controllers have control ids of 101 and 102, the setpoint controller id is 123.

The supervisor for the fuzzy controllers (label="S76_S352_Supervise") is defined in the rule file fcl="spvr_S76_S352.fcl" and has two control outputs (one for each controller) and four inputs. The output variables of the fuzzy controller supervisor are name="S76_Control" and name="S352_Control". These names match the definition of output variables (VAR_OUTPUT) in the spvr_S76_S352.fcl file. The ctrlID="101" and ctrlID="102" specify the controllers (listed in the <ctrlID>) that will have the output values applied to them. Since the func=controlOn", the output of the FCL variable S76_Control will be applied to the controller on/off attribute of the controller with the control id 101. The <varIn> environment couples the FCL file input variables (defined as VAR_INPUT in the FCL file) with the RSM state monitors.

The setpoint controller supervisor will modify the behavior of the controller with a control id of 123. The func="trigLow" specification means that the output value of the variable S340_Control_trigLow will be applied to set a new lower trigger threshold for the controller.

```
<management id="1" label="FuzzySupervisor">
 <fuz_supervise id="1" label="S76_S352_Supervise" fcl="spvr_S76_S352.fcl">
     <ctrlID> 101 102 </ctrlID>
    <varOut ctrlID="101" func="controlOn" name="S76_Control"></varOut>
     <varOut ctrlID="102" func="control0n" name="S352_Control"></varOut>
     <varIn name="S76_US441_Stage" monitor="segmentmonitor"</pre>
            monID="6"
                        monType="head"></varIn>
     <varIn name="S76_Stage"</pre>
                                    monitor="segmentmonitor"
           monID="7"
                        monType="head"></varIn>
     <varIn name="canalPoint_Stage" monitor="segmentmonitor"</pre>
           monID="142" monType="head"></varIn>
     <varIn name="S155_Stage"</pre>
                                    monitor="segmentmonitor"
           monID="78" monType="head"></varIn>
     <segmentmonitor id="6" attr="head"></segmentmonitor>
     <segmentmonitor id="7"</pre>
                             attr="head"></segmentmonitor>
     <segmentmonitor id="142" attr="head"></segmentmonitor>
     <segmentmonitor id="78" attr="head"></segmentmonitor>
  </fuz_supervise>
  <fuz_supervise id="2" label="S340_Supervise" fcl="spvr_S340.fcl">
     <ctrlID> 123 </ctrlID>
     <varOut ctrlID="123" func="triglow" name="S340_Control_trigLow"></varOut>
     <varIn name="S340_Stage" monitor="segmentmonitor" monID="363"</pre>
            monType="head"></varIn>
     <varIn name="season" monitor="tkprmonitor" monType="month"> </varIn>
     <segmentmonitor id="363" attr="head"></segmentmonitor>
     <tkprmonitor attr="month"></tkprmonitor>
  </fuz_supervise>
</management>
```

Following is an example of the FCL supervisor control file for supervision of the two fuzzy controllers.

```
FUNCTION_BLOCK S76_S352_Supervise
VAR_INPUT
        S76_US441_Stage : REAL;
       S76_Stage
                     : REAL;
        canalPoint_Stage : REAL;
        S155_Stage : REAL;
END_VAR
VAR_OUTPUT
        S76_Control : REAL;
       S352_Control : REAL;
END_VAR
FUZZIFY S76_US441_Stage
        // low ramp, med triangle, high ramp
        TERM low := (15, 1) (18, 0);
        TERM med := (15, 0) (18, 1) (20, 0);
        TERM high := (18, 0) (20, 1);
END_FUZZIFY
FUZZIFY S76_Stage
        // low ramp, med rectangle, high ramp
        TERM low := (15, 1) (18, 0);
        TERM med := (16, 0) (16, 1) (19, 1) (19, 0);
        TERM high := (18, 0) (20, 1);
END_FUZZIFY
FUZZIFY canalPoint_Stage
        // low ramp, med trapezoid, high ramp
        TERM low := (15, 1) (18, 0);
       TERM med := (15, 0) (16, 1) (18, 1) (20, 0);
        TERM high := (18, 0) (20, 1);
END_FUZZIFY
FUZZIFY S155_Stage
       // low ramp, med triangle, high ramp
        TERM low := (15, 1) (18, 0);
        TERM med := (15, 0) (18, 1) (20, 0);
        TERM high := (18, 0) (20, 1);
END_FUZZIFY
```

```
DEFUZZIFY S76_Control
          // All outputs are singletons
          TERM off := 0.;
          TERM on := 1.;
          RANGE
                   := (0, 1);
END_DEFUZZIFY
DEFUZZIFY S352_Control
          // All outputs are singletons
          TERM off := 0.;
          TERM on := 1.;
          RANGE
                   := (0, 1);
END_DEFUZZIFY
//
RULEBLOCK S76_S352_Rules
          RULE 1: IF S76_US441_Stage IS low OR S76_US441_Stage IS med
                  THEN S76_Control IS on;
          //
          RULE 2: IF S76_US441_Stage IS high
                  THEN S76_Control IS off;
          //
          RULE 3: IF S76_Stage IS low OR S76_Stage IS med
                  THEN S76_Control IS on;
          //
          RULE 4: IF S76_Stage IS high
                  THEN S76_Control IS off;
          //
          RULE 5: IF canalPoint_Stage IS low OR canalPoint_Stage IS med
                  THEN S352_Control IS on;
          //
          RULE 6: IF canalPoint_Stage IS high
                  THEN S352_Control IS off;
          RULE 7: IF S155_Stage IS low OR S155_Stage IS med
                  THEN S352_Control IS on;
          //
          RULE 8: IF S155_Stage IS high
                  THEN S352_Control IS off;
END_RULEBLOCK
END_FUNCTION_BLOCK
```

The following FCL shows an example of the fuzzy supervisor applied to the setpoint controller.

```
FUNCTION_BLOCK S340_Supervise
VAR_INPUT
        S340_Stage : REAL;
                 : REAL;
        season
END_VAR
VAR_OUTPUT
        S340_Control_trigLow : REAL;
END_VAR
FUZZIFY S340_Stage
        TERM low := (4, 1) (5, 0);
        TERM med := (4, 0) (5, 1) (6, 0);
        TERM high := (5, 0) (6, 1);
END_FUZZIFY
FUZZIFY season
        TERM dry1 := (4, 1) (4.1, 0);
        TERM wet := (4.5, 0) (4.5, 1) (9.5, 1) (9.5, 0);
        TERM dry2 := (9.9, 0) (10, 1);
END_FUZZIFY
DEFUZZIFY S340_Control_trigLow
        TERM one := 1.;
        TERM five := 5.;
                 := (0, 5);
       RANGE
END_DEFUZZIFY
RULEBLOCK S340_Rules
       RULE 1: IF S340_Stage IS low AND season is wet
                THEN S340_Control_trigLow IS one;
        RULE 2: IF S340_Stage IS low AND season is NOT wet
                THEN S340_Control_trigLow IS one;
        RULE 3: IF S340_Stage IS med AND season is wet
                THEN S340_Control_trigLow IS one;
        RULE 4: IF S340_Stage IS med AND season is NOT wet
                THEN S340_Control_trigLow IS five;
        RULE 5: IF S340_Stage IS high AND season is wet
                THEN S340_Control_trigLow IS five;
        RULE 6: IF S340_Stage IS high AND season is NOT wet
                THEN S340_Control_trigLow IS five;
END_RULEBLOCK
END_FUNCTION_BLOCK
```

10 GNU Linear Programming Kit (GLPK) Supervisor

RSM provides an interface to the GNU Linear Programming Kit (GLPK) [10]. The GLPK package is intended for solving large-scale linear programming (LP), mixed integer programming (MIP), and other related problems. It is a set of routines written in ANSI C and organized in the form of a callable library.

The GLPK package includes the following main components:

- Revised simplex method.
- Primal-dual interior point method.
- Branch-and-bound method.
- Translator for GNU MathProg.
- Application program interface (API).
- Stand-alone LP/MIP solver.

The GLPK distribution can be found in the subdirectory <code>/gnu/glpk/</code> on your favorite GNU mirror [10]. The GLPK documentation consists of the Reference Manual and the description of the GNU MathProg language. Both these documents are included in the distribution (in LaTeX, DVI, and PostScript formats).

10.1 GLPK MathProg Language

GLPK supports the GNU MathProg language, which is a subset of the AMPL language. AMPL is a comprehensive and powerful algebraic modeling language for linear and nonlinear optimization problems, in discrete or continuous variables. Developed at Bell Laboratories, AMPL lets you use common notation and familiar concepts to formulate optimization models and examine solutions, while the computer manages communication with an appropriate solver. (See www.ampl.com.)

10.2 GLPK Supervisor Usage

The RSM GLPK Supervisor (gplk_supervise) is defined by a MathProg model definition file which specifies the parameters, variables, and optimization function of the supervisor. The model definition file may also contain a data section which defines parametric values, and initial values for variables. If the data section is not included in the model definition file, then a separate data definition file must exist. The MSE GLPK supervisor reads these files, creates the GLPK problem objects, and calls the appropriate GLPK API routines to solve the supervisory constrained optimization problem.

Four information items have to be supplied to the supervisor for correct coupling to the RSM state and control information:

- 1. controller id's
- 2. input state variables
- 3. output control variables
- 4. GLPK model and data file(s)

this is done by use of the XML attributes available for the GLPK supervisor (glpk_supervise) shown in Table 10.2.

environment	attribute	meaning
<pre><glpk_supervise></glpk_supervise></pre>		
	id	supervisor id
	label	optional supervisor label
	modelFile	name of GLPK model file
	modelName	optional model label
	dataFile	name of GLPK data file
	probFile	optional problem output file
	solnFile	optional solution output file
	outputFile	optional info output file
	method	simplex or interior
	optimize	maximize or minimize
	presolve	on or off
	msglevel	0, 1, 2, 3
	timelimit	solution time limit in seconds
	outfreq	output info frequency in iterations
	days	supervise interval in days
	hours	supervise interval in hours
	minutes	supervise interval in minutes
<ctrlid></ctrlid>		list of controller IDs
<varin></varin>		input variable(s)
	param	MathProg parameter for input
	name	input variable name
	monitor	monitor specification
	monID	monitor ID
	monType	monitor type
<varout></varout>		output variable(s)
	ctrlID	controller ID
	wmID	watermover ID
	func	controller function
	name	output variable name
<pre><*monitor></pre>		State variable specification

Table 10.2. GLPK System XML $\,$

10.2.1 id attribute

The id is a unique supervisor identifier, label is an optional string which will label the outputs of the supervisor. modelName is an optional label

to name the GLPK problem internally, this name will then appear in the GLPK output files. The modelFile attribute must specify a valid GLPK MathProg model file. The dataFile is an optional file specification, if the GLPK model file contains a data section, this file is not required. If the model file does not have a data section, this attribute specifies the name of the data file.

10.2.2 probFile solnFile outputFile attributes

The probFile solnFile outputFile attributes define optionally created information files which contain plain text outputs of the GLPK problem statement, GLPK solution statement, and any runtime messages.

10.2.3 method attribute

Specification of the GLPK solution method is provided by the method attribute, which may be assigned one of the following values: simplex or interior, which enact either a two-phase revised simplex method, or a primal dual point interior method. Interior point methods are more modern and more powerful numerical methods for large scale linear programming. They work well for very sparse LP problems, and can solve such problems much more efficiently than simplex methods. The default is simplex.

10.2.4 optimize attribute

To specify the direction of the optimization, the user can set the optimize attribute to either maximize or minimize. The default is minimize.

10.2.5 presolve attribute

The simplex solver has a built in LP presolver, which is a subprogram that transforms the original LP problem to an equivalent LP problem which may be easier to solve than the original problem. Access to this feature is provided by the presolve attribute, which may be assigned the values of on or off, the default is off. This option is only useful for cases where a reoptimization is performed.

10.2.6 msglevel attribute

The user can control the level of message reporting from the GLPK solver with the msglevel attribute. The msglevel can be set to one of four values:

- 0 No messages
- 1 Error messages only
- 2 Normal messages
- 3 All messages

The default value is msglevel=1.

10.2.7 timelimit attribute

The timelimit attribute specifies the amount of time in seconds that the LP solution algorithm will be allowed to search for a solution. The default value is 1800 seconds.

10.2.8 outfreq

The outfreq attribute output defines the frequency in iterations of the LP solver at which solver output information is written. The default value is 200 iterations.

10.2.9 days hours minutes attribute

The supervisor time interval control attributes (days hours minutes) provide a mechanism to run the supervisor at selected intervals, see section 7.2.

10.2.10 ctrlID environment

The <ctrlID> environment defines a list of RSM controllers that will be supervised. The values in this list must match a cid= attribute of a valid controller definition. For example, if the following controller is defined:

```
<setpointctrl cid="125" wmID="25" label="S38 Culvert">
```

then a valid entry in the <ctrlID> list is 125. Each controller id in the list will have at least one corresponding <varOut> entry which couples the controller modifier with a corresponding GLPK problem variable defined in the GLPK model file.

10.2.11 varIn attributes

The <varIn> environment defines the HSE state input variables which will be linked to GLPK parameters defined in the GLPK model file. The name= arguments must correspond to a param defined in the GLPK model file. Each <varIn> entry will have an associated <*monitor> (i.e. <segmentmonitor>) entry. The monitor=, monID= and monType= attributes must match the attributes of the associated state <*monitor>. For example, the following are valid XML entries:

The corresponding data section of the GLPK model file could look like this:

where the parameter InitHead is a vector with multiple input parameters values IH_1 and IH_2.

If the input parameter is not a vector, but is a single variable, then the param and name attributes have the same argument, for example, if the GLPK data section has parameter entries as follows:

```
param IH_1 := 15 ;
param IH_2 := 17 ;
```

then the corresponding VarIn XML section would appear as:

If the monitor is a timekeeper monitor (<tkprmonitor>), the monID= attribute is not used. The timekeeper monitor does not use the id attribute as do the other state monitors. An example of this invocation would be:

10.2.12 varOut attributes

The <varOut> environments specify which controller is modified by which output variable in the GLPK model definition, or, activate a single controller for a watermover from among multiple controllers attached to a watermover. Section 5 details the allowable XML entities for <varOut>. In the case where a controller variable is to be changed, the ctrlID attribute is used to specify the controller, the name defines the the output variable name from the GLPK model file, and the func specifies the controller variable to be changed. It is possible to have multiple <varOut> entries for a single controller. For example, a supervisor may define three <varOut> terms to modify the on/off, minimum output, maximum output behaviors of a single controller. Each <varOut> would have a distinct func and name entry. Section 2.1 describes the available func attributes for each controller.

When a supervisor is used to activate a particular controller from among multiple controllers attached to a watermover, the wmID attribute is used to specify the affected watermover, the func="controller" must be set, and the name defines the output variable name from the GLPK model file which will return a controller id number (positive integer) of the controller to be activated.

An example of a valid VarOut XML section to change the attribute of a controller is shown below:

```
<varOut ctrlID="101" func="ControlOut" name="Gain_R1"> </varOut>
```

where the output value of the GLPK supervisor into the GLPK model variable named Gain_R1 is passed to the controller with id 101, and set as the new ControlOut value of the controller.

An example of a valid VarOut XML section to change the active controller of a watermover is shown below:

```
<varOut wmID="1" func="controller" name="wm1_ControllerID"> </varOut>
```

where the output of the GLPK supervisor into the GLPK model variable named wm1_ControllerID is a controller id, which is used to select a controller from the list of controllers attached to the watermover with wmID="1".

10.3 GLPK Supervisor Example

See the RSM Benchmark BM47 for a complete example of the GLPK supervisor applied to control of watermover controllers. An excerpt from the RSM XML file of BM47 is shown below.

10.3.1 GLPK XML File

```
<hse version="0.1">
  <control
   tslen="1"
   tstype="day"
   startdate="01jan2000"
   starttime="0000"
    enddate="30jan2000"
   endtime="0000"
   alpha="0.500"
   solver="PETSC"
   method="gmres"
   precond="ilu"
   units="METRIC"
   controllers="on"
   supervisors="on">
  </control>
  <mesh>
    <geometry file="mesh3x3.2dm"> </geometry>
    <shead> <gms file="hin3x3.dat"> </gms> </shead>
    <surface> <gms file="elev3x3.dat"> </gms> </surface>
    <bottom> <const value="-50.0"> </const> </bottom>
    <!-- Overland flow -->
    <conveyance> <mannings a="0.1" detent="0.00001"></mannings> </conveyance>
    <!-- Groundwater flow -->
    <transmissivity> <unconfined k = "0.001"> </unconfined> </transmissivity>
    <svconverter> <constsv sc="0.2"> </constsv> </svconverter>
  </mesh>
  <watermovers>
    <!-- R1 Release from 'lake' -->
    <setflow wmID="1" id1="2" id2="20" label="R1 Lake Release">
      <const value="30.0" dbintl="1440"> </const>
   </setflow>
   <!-- D1 Demand removed from 'wetland' -->
    <setflow wmID="2" id1="5" id2="21" label="D1 Demand">
       <const value="30.0" dbintl="1440"> </const>
    </setflow>
  </watermovers>
```

```
<!-- Controller Section -->
<controller id="1">
  <!-- Controller for R1 -->
  <lpctrl cid="101" wmID="1" label="FlowCtrl R1"> </lpctrl>
  <!-- Controller for D1 -->
  <lpctrl cid="102" wmID="2" label="FlowCtrl D1"> </lpctrl>
</controller>
<!-- Management Section -->
<management id="1" label="glpk_supervise">
  <glpk_supervise id="801" label="glpk_supervise"</pre>
  modelFile="glpk_mse.mod" modelName="nine_cell"
  probFile="_glpk_mse.prb" solnFile="_glpk_mse.sol" outputFile="_glpk_mse.out"
  method="simplex" optimize="minimize" presolve="off" msglevel="3"
  timelimit="60" outfreq="1000" days="7" hours="0" minutes="0">
     <!-- Controllers to be controlled -->
     <ctrlID> 101 102 </ctrlID>
     <!-- GLPK output variables to controllers -->
     <varOut ctrlID="101" func="ControlOut" name="Gain_R1"> </varOut>
     <varOut ctrlID="102" func="ControlOut" name="Gain_D1"> </varOut>
     <!-- Input variables to GLPK from HSE -->
     <varIn param="PCR1" name="PCR1" monitor="ctrlmonitor"</pre>
            monID="1" monType="maxflow"> </varIn>
     <varIn param="PCD1" name="PCD1" monitor="ctrlmonitor"</pre>
            monID="2" monType="maxflow"> </varIn>
     <varIn param="IH_1" name="IH_1" monitor="cellmonitor"</pre>
            monID="1" monType="head"> </varIn>
     <varIn param="IH_2" name="IH_2" monitor="cellmonitor"</pre>
            monID="2" monType="head"> </varIn>
     <!-- HSE State Monitors to VarIn variables -->
     <ctrlmonitor wmID="1" attr="maxflow"></ctrlmonitor>
     <ctrlmonitor wmID="2" attr="maxflow"></ctrlmonitor>
     <cellmonitor id="1" attr="head"></cellmonitor>
     <cellmonitor id="2" attr="head"></cellmonitor>
  </glpk_supervise>
</management>
```

</hse>

11 Graph Flow Algorithm Supervisor

Note: Currently, the flow results from a Graph supervisor are not output to the HSE watermovers or controllers.

From the perspective of mathematical graph theory, there is a well developed body of work regarding the assessment of flows in interconnected networks [11, 12]. Graph representations of flow networks for water distribution and stream flow networks are common, and useful [13, 14]. The MSE maintains a graph theory based representation of the managed canal network in the MSE Network, section 3. As described in the MSE Network section of the MSE Controllers Manual, the MSE Network may be defined with an XML file, or a flat-file representation.

The Graph supervisor implements the maxflow, feasible flow, and mincost feasible flow algorithms. These algorithms are highly efficient numerical procedures which solve constrained optimization problems on the network flow by taking advantage of the network properties, rather than by solving a set of simultaneous equations explicitly. The constraints consist of the canal arc capacity, the hydraulic structure capacity, demand and supply flows at the structures, and flow cost weights assigned to the canal arcs.

Each graph supervisor solves the network flow based on it's own MSE Network representation, however, this representation can be degenerate with other supervisor MSE Network representations, therefore supervisors may share the same MSE Network representation. As a result, a graph supervisor can solve the flow for the entire network, or for any subset of the network for which a graph has been defined.

11.1 Graph Flow Supervisor XML

XML attributes available for the Graph flow supervisor are shown in Table 11.1.

environment	attribute	meaning
<pre><graph_supervise></graph_supervise></pre>		
	id	supervisor id
	label	optional supervisor label
	xml	MSE Network XML file
	graph	MSE Network flat file
	flow	flow solution type
	days	supervise interval in days
	hours	supervise interval in hours
	minutes	supervise interval in minutes
<ctrlid></ctrlid>		list of controller IDs

Table 11.1. Graph Flow XML

11.1.1 graph supervise attributes

The id is a unique supervisor identifier, label is an optional string which will label the outputs of the supervisor. The xml attribute can specify a valid MSE Network XML file, refer to the MSE Network XML section of the Controllers Manual. Alternatively, the graph attribute can define a flat-file MSE Network representation, see the MSE Network Flat File section of the Controllers Manual. The flow attribute can be set to feasible or maxflow (the default). The supervisor time interval control attributes (days hours minutes) provide a mechanism to run the supervisor at selected intervals, see section 7.2.

11.2 Graph Supervise Example

An example XML entry for two graph supervisors is shown below. The first supervisor is reads it's MSE Network representation from the flat file maxflow_fig22.28.dat and computes a maxflow solution. The second example reads it's MSE Network from the XML file mse_network.xml and computes a feasible flow solution.

12 Object Routing Model-Assessor Supervisor

The ORM supervisor is currently under development. The functionality of the ORM is being decomposed into a suite of Assessors. Refer to benchmark BM63 for the latest information on this development.

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